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Note that this last matrix is equal to the Hessian of the objective function when the problem is unconstrained (m = 0), which autorizes us to use the same symbol **H** for both cases.

Full advantage can be taken of any zero coefficients in the matrices H or J.

The module also contains subroutines that are designed for printing parts of the problem data, and for matrix storage scheme conversions.

ATTRIBUTES — Versions: GALAHAD_NLPT_single, GALAHAD_NLPT_double, Calls: GALAHAD_TOOLS. Date: May 2003. Origin: N. I. M. Gould, Rutherford Appleton Laboratory, and Ph. L. Toint, University of Namur, Belgium. Language: Fortran 95 + TR 15581 or Fortran 2003.

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where y belongs to \mathbb{R}^m and z belongs to \mathbb{R}^n . The solution of such problem may require the storage of the objective function's gradient

 $\mathbf{H}_f(\mathbf{x}) = \nabla_{\mathbf{x}\mathbf{x}}\mathbf{f}(\mathbf{x})$

 $\mathbf{g}(\mathbf{x}) = \nabla_{\mathbf{x}} \mathbf{f}(\mathbf{x}),$

the $n \times n$ symmetric objective function's Hessian

the $m \times n$ constraints' Jacobian whose *i*-th row is the gradient of the *i*-th constraint:

 $\mathbf{e}_i^T \mathbf{J}(\mathbf{x}) = [\nabla_{\mathbf{x}} \mathbf{c}_i(\mathbf{x})]^T,$

the gradient of the Lagrangian with respect to x,

 $\mathbf{g}_L(\mathbf{x},\mathbf{y},\mathbf{z}) = \nabla_{\mathbf{x}} \mathbf{L}(\mathbf{x},\mathbf{y},\mathbf{z})$

and of the Lagrangian's Hessian with respect to x

 $\mathbf{H}_{L}(\mathbf{x},\mathbf{y},\mathbf{z}) = \nabla_{\mathbf{x}\mathbf{x}}\mathbf{L}(\mathbf{x},\mathbf{y},\mathbf{z}).$

where f ities are understood componentwise. The vectors $\mathbf{c}^l \leq \mathbf{c}^u$ and $\mathbf{x}^l \leq \mathbf{x}^u$ are *m*- and *n*-dimensional, respectively, and may contain components equal to minus or plus infinity. An important function associated with the problem is its Lagrangian

$$\mathbf{L}(\mathbf{x}, \mathbf{y}, \mathbf{z}) = \mathbf{f}(\mathbf{x}) - \mathbf{y}^T \mathbf{c}(\mathbf{x}) - \mathbf{z}^T \mathbf{x}$$

$$\mathbf{x}^{l} \leq \mathbf{x} \leq \mathbf{x}^{u}$$
,
'is a smooth "objective function", where $\mathbf{c}(x)$ is a smooth function from \mathbb{R}^{n} into \mathbb{R}^{m} and where inequal

This package defines a derived type capable of supporting the storage of a variety of smooth nonlinear programming

 $\min \mathbf{f}(\mathbf{x})$

 $\mathbf{c}^l < \mathbf{c}(\mathbf{x}) < \mathbf{c}^u$,

USER DOCUMENTATION

SUMMARY

problems of the form

subject to the general constraints

1

and





NLPT

GALAHAD Optimization Library version 5.0

NLPT

2 HOW TO USE THE PACKAGE

The package is available using both single and double precision reals, and either 32-bit or 64-bit integers. Access to the 32-bit integer, single precision version requires the USE statement

```
USE GALAHAD_NLPT_single
```

with the obvious substitution GALAHAD_NLPT_double, GALAHAD_NLPT_single_64 and GALAHAD_NLPT_double_64 for the other variants.

If it is required to use more than one of the modules at the same time, the derived type NLPT_problem_type, (Section 2.4) must be renamed on one of the USE statements.

2.1 Matrix storage formats

Both the Hessian matrix \mathbf{H} and the Jacobian \mathbf{J} may be stored in one of three input formats (the format for the two matrices being possibly different).

2.1.1 Dense storage format

The matrix **J** is stored as a compact dense matrix by rows, that is, the values of the entries of each row in turn are stored in order within an appropriate real one-dimensional array. Component n * (i-1) + j of the storage array J_val will hold the value J_{ij} for i = 1, ..., m, j = 1, ..., n. Since **H** is symmetric, only the lower triangular part (that is the part h_{ij} for $1 \le j \le i \le n$) need be held. In this case the lower triangle will be stored by rows, that is component i * (i-1)/2 + j of the storage array H_val will hold the value h_{ij} (and, by symmetry, h_{ji}) for $1 \le j \le i \le n$. If this storage scheme is used, J_type and/or H_type must be set the value of the symbol GALAHAD_DENSE.

2.1.2 Sparse co-ordinate storage format

Only the nonzero entries of the matrices are stored. For the *l*-th entry of **J**, its row index *i*, column index *j* and value J_{ij} are stored in the *l*-th components of the integer arrays J_row, J_col and real array J_val. The order is unimportant, but the total number of entries J_ne is also required. The same scheme is applicable to **H** (thus requiring integer arrays H_row, H_col, a real array H_val and an integer value H_ne), except that only the entries in the lower triangle need be stored.

If this storage scheme is used, J_type and/or H_type must be set the value of the symbol GALAHAD_COORDINATE.

2.1.3 Sparse row-wise storage format

Again only the nonzero entries are stored, but this time they are ordered so that those in row *i* appear directly before those in row i+1. For the *i*-th row of **J**, the *i*-th component of a integer array J_ptr holds the position of the first entry in this row, while J_ptr (m+1) holds the total number of entries plus one. The column indices *j* and values J_{ij} of the entries in the *i*-th row are stored in components $l = J_ptr(i), \ldots, J_ptr(i+1) - 1$ of the integer array J_col, and real array J_val, respectively. The same scheme is applicable to **H** (thus requiring integer array H_ptr, H_col, and a real array H_val), except that only the entries in the lower triangle need be stored. The values of J_ne and H_ne are not mandatory, since they can be recovered from

$$J_ne = J_ptr(n+1) - 1$$
 and $H_ne = H_ptr(n+1) - 1$

For sparse matrices, this scheme almost always requires less storage than its predecessor.

If this storage scheme is used, J_type and/or H_type must be set the value of the symbol GALAHAD_SPARSE_BY_ROWS.

GALAHAD

2.2 Optimality conditions

The solution **x** necessarily satisfies the primal first-order optimality conditions

$$\mathbf{c}^l \leq \mathbf{c}(\mathbf{x}) \leq \mathbf{c}^u$$
, and $\mathbf{x}^l \leq \mathbf{x} \leq \mathbf{x}^u$,

the dual first-order optimality conditions

$$\mathbf{g}(\mathbf{x}) = \mathbf{J}(\mathbf{x})^T \mathbf{y} + \mathbf{z}$$

where

$$\mathbf{y} = \mathbf{y}^l + \mathbf{y}^u, \ \mathbf{z} = \mathbf{z}^l + \mathbf{z}^u \ \mathbf{y}^l \ge 0, \ \mathbf{y}^u \le 0, \ \mathbf{z}^l \ge 0 \ \text{and} \ \mathbf{z}^u \le 0,$$

and the complementary slackness conditions

$$(\mathbf{c}(\mathbf{x})-\mathbf{c}^l)^T\mathbf{y}^l=0, \ (\mathbf{c}(\mathbf{x})-\mathbf{c}^u)^T\mathbf{y}^u=0, \ (\mathbf{x}-\mathbf{x}^l)^T\mathbf{z}^l=0 \ \text{and} \ (\mathbf{x}-\mathbf{x}^u)^T\mathbf{z}^u=0,$$

where the vectors \mathbf{y} and \mathbf{z} are known as the Lagrange multipliers for the general constraints, and the dual variables for the bounds, respectively, and where the vector inequalities hold componentwise. The dual first-order optimality condition is equivalent to the condition that $\mathbf{g}_L(\mathbf{x}, \mathbf{y}, \mathbf{z}) = 0$.

2.3 Real and integer kinds

We use the terms integer and real to refer to the fortran keywords REAL(rp_{-}) and INTEGER(ip_{-}), where rp_{-} and ip_{-} are the relevant kind values for the real and integer types employed by the particular module in use. The former are equivalent to default REAL for the single precision versions and DOUBLE PRECISION for the double precision cases, and correspond to rp_{-} = real32 and rp_{-} = real64, respectively, as supplied by the fortran iso_fortran_env module. The latter are default (32-bit) and long (64-bit) integers, and correspond to ip_{-} = int32 and ip_{-} = int64, respectively, again from the iso_fortran_env module.

2.4 The derived data type

A single derived data type, NLPT_problem_type, is accessible from the package. It is intended that, for any particular application, only those components which are needed will be set. The components are:

pname is a scalar variable of type default CHARACTER (LEN = 10), that holds the problem's name.

- n is a scalar variable of type INTEGER (ip_), that holds the number of optimization variables, n.
- vnames is a rank-one allocatable array of dimension n and type CHARACTER (LEN = 10) that holds the names of the problem's variables. The *j*-th component of vnames, j = 1, ..., n, contains the name of x_j .
- x is a rank-one allocatable array of dimension n and type REAL (rp_), that holds the values **x** of the optimization variables. The *j*-th component of x, j = 1, ..., n, contains x_j .
- x_l is a rank-one allocatable array of dimension n and type REAL (rp_), that holds the vector of lower bounds \mathbf{x}^l on the variables. The *j*-th component of x_l, j = 1, ..., n, contains \mathbf{x}_j^l . Infinite bounds are allowed by setting the corresponding components of x_l to any value smaller than -infinity.
- x_u is a rank-one allocatable array of dimension n and type REAL (rp_), that holds the vector of upper bounds \mathbf{x}^u on the variables. The *j*-th component of x_u, j = 1, ..., n, contains \mathbf{x}_j^u . Infinite bounds are allowed by setting the corresponding components of X_u to any value larger than that infinity.
- z is a rank-one allocatable array of dimension n and type default REAL (rp_), that holds the values z of estimates of the dual variables corresponding to the simple bound constraints (see Section 2.2). The *j*-th component of z, j = 1, ..., n, contains z_j .

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- x_status is a rank-one allocatable array of dimension n and type INTEGER (ip_), that holds the status of the problem's variables corresponding to the presence of their bounds. The *j*-th component of x_status, j = 1, ..., n, contains the status of x_j . Typical values are GALAHAD_FREE, GALAHAD_LOWER, GALAHAD_UPPER, GALAHAD_RANGE, GALAHAD_FIXED, GALAHAD_STRUCTURAL, GALAHAD_ELIMINATED, GALAHAD_ACTIVE, GALAHAD_INACTIVE or GALAHAD_UNDEFINED.
- f is a scalar variable of type REAL (rp_), that holds the current value of the objective function.
- g is a rank-one allocatable array of dimension n and type REAL (rp_), that holds the gradient **g** of of the objective function. The *j*-th component of g, j = 1, ..., n, contains g_j .
- H_type is a scalar variable of type INTEGER(ip_), that specifies the type of storage used for the lower triangle of the objective function's or Lagrangian's Hessian **H** Possible values are GALAHAD_DENSE, GALAHAD_COORDINATE or GALAHAD_SPARSE_BY_ROWS.
- H_ne is a scalar variable of type INTEGER (ip_), that holds the number of non-zero entries in the lower triangle of the objective function's or Lagrangian's Hessian **H**.
- H_val is a rank-one allocatable array of type REAL (rp_), that holds the values of the entries of the **lower triangular** part of the Hessian matrix **H** in any of the storage schemes discussed in Section 2.1.
- H_row is a rank-one allocatable array of type INTEGER (ip_), that holds the row indices of the **lower triangular** part of **H** in the sparse co-ordinate storage scheme (see Section 2.1.2). It need not be allocated for either of the other two schemes.
- H_col is a rank-one allocatable array variable of type INTEGER (ip_), that holds the column indices of the **lower triangular** part of **H** in either the sparse co-ordinate (see Section 2.1.2), or the sparse row-wise (see Section 2.1.3) storage scheme. It need not be allocated when the dense storage scheme is used.
- H_ptr is a rank-one allocatable array of dimension n+1 and type INTEGER(ip_), that holds the starting position of each row of the **lower triangular** part of **H**, as well as the total number of entries plus one, in the sparse row-wise storage scheme (see Section 2.1.3). It need not be allocated when the other schemes are used.
- m is a scalar variable of type INTEGER (ip_), that holds the number of general linear constraints, m.
- c is a rank-one allocatable array of dimension m and type default REAL (rp_), that holds the values $\mathbf{c}(\mathbf{x})$ of the constraints. The *i*-th component of c, i = 1, ..., m, contains $\mathbf{c}_i(\mathbf{x})$.
- c_l is a rank-one allocatable array of dimension m and type REAL (rp_), that holds the vector of lower bounds \mathbf{c}^l on the general constraints. The *i*-th component of c_l, i = 1, ..., m, contains \mathbf{c}_i^l . Infinite bounds are allowed by setting the corresponding components of c_l to any value smaller than -infinity.
- c_u is a rank-one allocatable array of dimension m and type REAL (rp_), that holds the vector of upper bounds \mathbf{c}^{u} on the general constraints. The *i*-th component of c_u, i = 1, ..., m, contains \mathbf{c}_{i}^{u} . Infinite bounds are allowed by setting the corresponding components of c_u to any value larger than infinity.
- equation is a rank-one allocatable array of dimension m and type default LOGICAL, that specifies if each constraint is an equality or an inequality. The *i*-th component of equation is .TRUE. iff the *i*-th constraint is an equality, i.e. iff $\mathbf{c}_i^l = \mathbf{c}_i^u$.
- linear is a rank-one allocatable array of dimension m and type default LOGICAL, that specifies if each constraint is linear. The *i*-th component of linear is .TRUE. iff the *i*-th constraint is linear.
- y is a rank-one allocatable array of dimension m and type REAL (rp_), that holds the values y of estimates of the Lagrange multipliers corresponding to the general constraints (see Section 2.2). The *i*-th component of y, i = 1, ..., m, contains y_i .

- c_status is a rank-one allocatable array of dimension m and type INTEGER (ip_), that holds the status of the problem's constraints corresponding to the presence of their bounds. The *i*-th component of c_status, j = 1, ..., m, contains the status of c_i . Typical values are GALAHAD_FREE, GALAHAD_LOWER, GALAHAD_UPPER, GALAHAD_RANGE, GALAHAD_FIXED, GALAHAD_STRUCTURAL, GALAHAD_ELIMINATED, GALAHAD_ACTIVE, GALAHAD_INACTIVE or GALAHAD_UNDEFINED.
- J_type is a scalar variable of type INTEGER (ip_), that specifies the type of storage used for the constraints' Jacobian J. Possible values are GALAHAD_DENSE, GALAHAD_COORDINATE or GALAHAD_SPARSE_BY_ROWS.
- J_ne is a scalar variable of type INTEGER (ip_), that holds the number of non-zero entries in the constraints' Jacobian J.
- J_val is a rank-one allocatable array of type REAL (rp_), that holds the values of the entries of the Jacobian matrix J in any of the storage schemes discussed in Section 2.1.
- J_row is a rank-one allocatable array of type INTEGER (ip_), that holds the row indices of **J** in the sparse co-ordinate storage scheme (see Section 2.1.2). It need not be allocated for either of the other two schemes.
- J_col is a rank-one allocatable array variable of type INTEGER (ip_), that holds the column indices of J in either the sparse co-ordinate (see Section 2.1.2), or the sparse row-wise (see Section 2.1.3) storage scheme. It need not be allocated when the dense storage scheme is used.
- J_ptr is a rank-one allocatable array of dimension m+1 and type INTEGER(ip_), that holds the starting position of each row of **J**, as well as the total number of entries plus one, in the sparse row-wise storage scheme (see Section 2.1.3). It need not be allocated when the other schemes are used.
- gL is a rank-one allocatable array of dimension n and type REAL (rp_), that holds the gradient \mathbf{g}_L of of the problem's Lagrangian L with respect to x. The *j*-th component of gL, j = 1, ..., n, contains $[\mathbf{g}_L]_j$.

Note that not every component of this data type is used by every package.

2.5 Argument lists and calling sequences

There are seven procedures for user calls:

- 1. The subroutine NLPT_write_stats is used to write general information on the problem such as the number of variables and constraints of different types.
- 2. The subroutine NLPT_write_variables is used to write the current values of the problem's variables, bounds and of their associated duals.
- 3. The subroutine NLPT_write_constraints is used to write the current values of the problem's constraints, bounds and of their associated multipliers.
- 4. The subroutine NLPT_write_problem is used to write the problem's number of variables and constraints per type, as well as current values of the problem's variables and constraints. This broadly corresponds to successively calling the three subroutines mentioned above. The subroutine additionally (optionally) writes the values of the Lagrangian's Hessian **H** and constraints Jacobian **J**.
- 5. The subroutine NLPT_J_from_C_to_Srow builds the permutation that transforms the Jacobian from coordinate storage to sparse-by-row storage, as well as the J_ptr and J_col vectors.
- 6. The subroutine NLPT_J_from_C_to_Scol builds the permutation that transforms the Jacobian from coordinate storage to sparse-by-column storage, as well as the J_ptr and J_row vectors.
- 7. The subroutine NLPT_cleanup is used to deallocate the memory space used by a problem data structure.

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2.5.1 Writing the problem's statistics

The number of variables and constraints for each type of bounds (free, lower/upper bounded, range bounded, linear, equalities/fixed) is output by using the call

```
CALL NLPT_write_stats( problem, out )
```

where

- problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the problem for which statistics must be written.
- out is a scalar INTENT (IN) argument of type INTEGER (ip_), that holds the device number on which problem statistics should be written.

Note that problem%pname is assumed to be defined and that both problem%c_l and problem%c_u are assumed to be associated whenever problem%m > 0.

2.5.2 Writing the problem's variables, bounds and duals

The values of the variables and associated bounds and duals is output by using the call

CALL NLPT_write_variables(problem, out)

where

- problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the problem for which variables values, bounds and duals must be written.
- out is a scalar INTENT (IN) argument of type INTEGER (ip_), that holds the device number on which problem variables values, bounds and duals should be written.

This routine assumes that problem%pname and problem%x are associated. The bounds are printed whenever problem%x_l and problem%x_u are associated. Moreover, it is also assumed in this case that problem%g is associated when problem%m = 0, and that problem%z is associated when problem%m > 0. The variables' names are used whenever problem%vnames is associated, but this is not mandatory.

2.5.3 Writing the problem's constraints, bounds and multipliers

The values of the constraints and associated bounds and multipliers is output by using the call

```
CALL NLPT_write_constraints( problem, out )
```

where

- problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the problem for which constraints values, bounds and multipliers must be written.
- out is a scalar INTENT (IN) argument of type INTEGER (ip_), that holds the device number on which problem constraints values, bounds and multipliers should be written.

This routine assumes that problem%pname, problem%c problem%c_l, problem%c_u and problem%y are associated. The types of constraints are used whenever problem%equation and/or problem%linear are associated, but this is not mandatory. The constraints' names are used whenever problem%cnames is associated, but this is not mandatory.

The most important data of a problem can be output by the call

```
CALL NLPT_write_problem( problem, out, print_level )
```

where

- problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the problem whose data must be written.
- out is a scalar INTENT(IN) argument of type INTEGER(ip_), that holds the device number on which the problem data should be written.
- print_level is a scalar INTENT(IN) argument of type INTEGER(ip_), that holds the level of details required for output. Possible values are:

GALAHAD_SILENT: no output is produced;

- GALAHAD_TRACE: the problem's statistics are output, plus the norms of the current vector of variables, the objective function's value and the norm of its gradient, and the maximal bound and constraint violations.
- GALAHAD_ACTION: the problem's statistics are output, plus the values of the variables, bounds and associated duals, the value of the objective function, the value of the objective function's gradient, the values of the constraints and associated bounds and multipliers.
- GALAHAD_DETAILS: as for GALAHAD_ACTION, plus the values of the Lagrangian's Hessian and of the constraints' Jacobian.

This routine assumes that problem%pname and problem%x are associated. The bounds on the variables are printed whenever problem%x_l and problem%x_u are associated. Moreover, it is also assumed in this case that problem%g is associated when problem%m = 0, and that problem%z is associated when problem%m > 0. The variables' names are used whenever problem%vnames is associated, but this is not mandatory. In the case where problem%m > 0, it is furthermore assumed that problem%c problem%c_l, problem%c_u and problem%y are associated. The types of constraints are used whenever problem%equation and/or problem%linear are associated, but this is not mandatory. The constraints' names are used whenever problem%cnames is associated, but this is not

2.5.5 Problem cleanup

The memory space allocated to allocatable in the problem data structure is deallocated by the call

```
CALL NLPT_cleanup( problem )
```

where

problem is a scalar INTENT (IN) argument of type NLPT_problem_type, that holds the problem whose memory space must be deallocated.

2.5.6 Transforming the Jacobian from co-ordinate storage to sparse-by-rows

The permutation that transforms the Jacobian from co-ordinate storage to sparse-by-rows, as well as the associated ptr and col vectors can be obtained by the call

CALL NLPT_J_perm_from_C_to_Srow(problem, perm, col, ptr)

where

problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the Jacobian matrix to transform. Note that we must have problem%J_type = GALAHAD_COORDINATE.

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- perm is an allocatable to a vector INTENT (OUT) of type INTEGER(ip_) and dimension equal to problem%J_nnz, that returns the permutation of the elements of problem%J_val that must be applied to transform the Jacobian from co-ordinate storage to sparse-by-rows.
- col is an allocatable to a vector INTENT(OUT) of type INTEGER(ip_) and dimension problem%J_ne whose k-th component is the column index of the k-th element of problem%J_val after permutation by perm.
- ptr is an allocatable to a vector INTENT(OUT) of type INTEGER(ip_) and dimension problem%m +1 whose *i*-the component is the index in problem%J_val (after permutation by perm) of the first entry of row *i*. Moreover,

 $ptr(problem\%m+1) = problem\%J_ne+1.$

2.5.7 Transforming the Jacobian from co-ordinate storage to sparse-by-columns

The permutation that transforms the Jacobian from co-ordinate storage to sparse-by-columns, as well as the associated ptr and row vectors can be obtained by the call

CALL NLPT_J_perm_from_C_to_Scol(problem, perm, row, ptr)

where

- problem is a scalar INTENT(IN) argument of type NLPT_problem_type, that holds the Jacobian matrix to transform. Note that we must have problem%J_type = GALAHAD_COORDINATE.
- perm is an allocatable to a vector INTENT (OUT) of type INTEGER (ip_) and dimension equal to problem%J_nnz, that returns the permutation of the elements of problem%J_val that must be applied to transform the Jacobian from co-ordinate storage to sparse-by-columns.
- col is an allocatable to a vector INTENT(OUT) of type INTEGER(ip_) and dimension problem%J_ne whose k-th component is the row index of the k-th element of problem%J_val after permutation by perm.
- ptr is an allocatable to a vector INTENT(OUT) of type INTEGER(ip_) and dimension problem%m +1 whose *i*-the component is the index in problem%J_val (after permutation by perm) of the first entry of column *i*. Moreover,

 $ptr(problem\%m+1) = problem\%J_ne+1.$

3 GENERAL INFORMATION

Other modules used directly: None.

Other routines called directly: NLPT_solve calls the BLAS functions *NRM2, where * is S for the default real version and D for the double precision version.

Other modules used directly: NLPT calls the TOOLS GALAHAD module.

Input/output: Output is under the control of the print_level argument for the NLPT_write_problem subroutine.

Portability: ISO Fortran 95 + TR 15581 or Fortran 2003. The package is thread-safe.

🜌 GALAHAD

4 EXAMPLE OF USE

Suppose we wish to present the data for the problem of minimizing the objective function $(\mathbf{x}_1 - 2)\mathbf{x}_2$ subject to the constraints $\mathbf{x}_1^2 + \mathbf{x}_2^2 \le 1$, $0 \le -\mathbf{x}_1 + \mathbf{x}_2$, and the simple bound $0 \le \mathbf{x}_1$, where the values are computed at the point $\mathbf{x}^T = (0, 1)$, which, together with the values $z_1 = 1$ and $\mathbf{y}^T = (-1, 0)$ defines a first-order critical point for the problem. Assume that we wish to store the Lagrangian's Hessian and the Jacobian in co-ordinate format. Assume also that we wish to write this data. We may accomplish these objectives by using the code:

```
PROGRAM GALAHAD NLPT EXAMPLE
 USE GALAHAD_NLPT_double ! the problem type
 USE GALAHAD_SYMBOLS
 IMPLICIT NONE
                                  :: wp = KIND( 1.0D+0 )
 INTEGER, PARAMETER
 INTEGER, PARAMETER :: iout = 6 ! stdout and stderr
 REAL( KIND = wp ), PARAMETER
                                  :: INFINITY = (10.0_wp)**19
 TYPE( NLPT_problem_type )
                                   :: problem
! Set the problem up.
 problem%pname = 'NLPT-TEST'
 problem%infinity = INFINITY
 problem%n
                  = 2
 ALLOCATE ( problem%vnames ( problem%n ), problem%x ( problem%n )
                                                                               &
           problem%x_l( problem%n ) , problem%x_u( problem%n ),
                                                                               8
                                      , problem%z( problem%n ) )
           problem%g( problem%n )
               = 2
 problem%m
 ALLOCATE( problem%equation( problem%m ), problem%linear( problem%m ),
                                                                               8
            problem%c( problem%m ) , problem%c_l( problem%m ),
                                                                               æ
           problem%c_u( problem%m), problem%y( problem%m ),
                                                                               8
           problem%cnames( problem%m ) )
 problem%J_ne = 4
 ALLOCATE ( problem%J_val ( problem%J_ne ), problem%J_row ( problem%J_ne ),
                                                                               8
           problem%J_col( problem%J_ne ) )
  problem%H_ne = 3
  ALLOCATE( problem%H_val( problem%H_ne ), problem%H_row( problem%H_ne ),
                                                                               8
           problem%H_col( problem%H_ne ) )
 problem%H_type = GALAHAD_COORDINATE
 problem%J_type = GALAHAD_COORDINATE
 problem%vnames = (/ 'X1' , 'X2'
                                            /)
 problem%x = (/ 0.0D0 , 1.0D0 /)
problem%x_1 = (/ 0.0D0 , -INFINITY /)
problem%x_u = (/ INFINITY, INFINITY /)
                         0.0D0 ,
                        INFINI.
'C1', 'C2
'C0, 1.0D0
 problem%cnames = (/ 'C1', 'C2'
problem%c = (/ 0.0D0, 1.0D0
problem%c_l = (/ -INFINITY, 0.0D0
                                    'C2' /)
                                            /)
                                           /)
 problem%c_u = (/ 1.0D0 , INFINITY /)
problem%y = (/ -1.0D0 , 0.0D0 /)
 problem%equation = (/ .FALSE. , .FALSE. /)
 problem%linear = (/ .FALSE. ,
                                   .TRUE. /)
 problem%z = (/ 1.0D0 ,
                                   0.0D0 /)
 problem%f = -2.0_wp
problem%g = (/ 1.0D0 , -1.0D0
                                           /)
 problem%J_row = (/
                                                   2
                         1 , 1
                                                              2.
                                                                    /)
                                            ,
                                                         1
 problem%J_col = (/
                         1
                                     2
                                                  1
                                                              2
                                                                    /)
 problem%J_val = (/ 0.0D0 , 2.0D0 ,
                                               -1.0D0
                                                             1.0D0
                                                                    /)
 problem%H_row = (/ 1 ,
                                   2
                                                 2
                                                        /)
                                            ,
 problem%H_col = (/ 1
                                      1
                                                   2
                                                         /)
```

NLPT

NULLIFY(problem%x_status, problem%H_ptr, problem%J_ptr, problem%gL) CALL NLPT_write_problem(problem, iout, GALAHAD_DETAILS) ! Cleanup the problem. CALL NLPT_cleanup(problem) STOP END PROGRAM GALAHAD_NLPT_EXAMPLE which gives the following output: +-----+ Problem : NLPT-TEST 1 1 +-----+ Free Lower Upper Range Fixed/ Linear Total bounded bounded bounded equalities Variables Constraints _____ Problem : NLPT-TEST -----+ Lower j Name Value Upper Dual value 0.0000E+00 0.0000E+00 1 X1 1.0000E+00 1.0000E+00 2 X2 OBJECTIVE FUNCTION value = -2.0000000E+00 GRADIENT of the objective function: 1 1.000000E+00 -1.000000E+00 Lower triangle of the HESSIAN of the Lagrangian: i j value i j value i j value 1 1 2.0000E+00 2 1 1.0000E+00 2 2 2.0000E+00 _____ Problem : NLPT-TEST i Name Lower Value Upper Dual value 0.0000E+00 1.0000E+00 -1.0000E+00 1 C1 2 C2 0.0000E+00 1.0000E+00 0.0000E+00 linear

problem%H_val = (/ 2.0D0 , 1.0D0 , 2.0D0 /)

🜌 GALAHAD

JACOBIAN matrix:

UNCODIAN MALTIA.								
i	j	value	i	j	value	i	j	value
1 2		.0000E+00 .0000E+00	1	2	2.0000E+00	2	1	-1.0000E+00
			END	OF PF	OBLEM			
We could choose to hold the lower triangle of \mathbf{H} is sparse-by-rows format by replacing the lines								
ALLOCATE(problem%H_val(problem%H_ne), problem%H_row(problem%H_ne), & problem%H_col(problem%H_ne)) problem%H_type = GALAHAD_COORDINATE								
and								
probl probl	em%H_col em%H_val	<pre>y = (/ = (/ = (/ 2. blem%x_status,</pre>	1 , .ODO ,	1 1.00		. ,	lem%ç	łr)
by								
ALLOCATE(problem%H_val(problem%H_ne), problem%H_col(problem%H_ne), & problem%H_ptr(problem%n + 1)) problem%H_type = GALAHAD_SPARSE_BY_ROWS								
and								
probl	em%H_val	= (/ = (/ = (/ 2. blem%x_status,	.ODO ,	1.00	, 2	. ,	lem%c	łr)
or using a dense storage format with the replacement lines								
ALLOCATE(problem%H_val(((problem%n + 1) * problem%n) / 2)) problem%H_type = GALAHAD_DENSE								
and								
-	FY(prob	= (/ 2. plem%x_status, plem%J_ptr, pr	problem	m%H_rc	0 , 2.0D0 w, problem%H_c	/) ol, prob	lem%H	l_ptr, &

respectively.

For examples of how the derived data type NLPT_problem_type may be used in conjunction with the GALAHAD nonlinear feasibility code, see the specification sheets for the GALAHAD_FILTRANE package.